

# *Gratings: Theory and Numeric Applications*

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## **E Popov, Chapter 7: Differential Theory of Periodic Structures**

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